



Number Fluctuations of Sparse Quasiparticles in a Superconductor

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Properties of a superconductor

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- \bullet Presence of a energy gap in the spectrum Δ
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At $T \approx 0$ $\frac{[\Delta(0) - \Delta(T)]}{\Delta(0)} \approx e^{-\Delta(0)/kT}$













Quasiparticle dynamics

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Recombination time



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D.C. Mattis and J. Bardeen Phys. Rev. 111, 412 (1958)









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- Complex transmission measured











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Roll-off in the noise spectrum determined solely by τ_r























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- Below 160 mK, $\tau_r \approx 2.2 \text{ ms}$
- τ₀ ≈ 460 ns

 is extracted with a fit











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 Qp generation by the microwave signal










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- Observed saturation of n_{qp} at low T
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- Residual ("nonequilibrium") qp concluded

