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Non-Fermi-liquid *d*-wave metal phase of strongly interacting electrons

Hong-Chen Jiang¹, Matthew S. Block², Ryan V. Mishmash³, James R. Garrison³, D. N. Sheng⁴, Olexei I. Motrunich⁵ & Matthew P. A. Fisher³

Developing a theoretical framework for conducting electronic fluids qualitatively distinct from those described by Landau's Fermi-liquid theory is of central importance to many outstanding problems in condensed matter physics. One such problem is that, above the transition temperature and near optimal doping, high-transition-temperature copper-oxide superconductors exhibit 'strange metal' behaviour that is inconsistent with being a traditional Landau Fermi liquid. Indeed, a microscopic theory of a strange-metal quantum phase could shed new light on the interesting low-temperature behaviour in the pseudogap regime and on the *d*-wave superconductor itself. Here we present a theory for a specific example of a strange metal-the 'd-wave metal'. Using variational wavefunctions, gauge theoretic arguments, and ultimately large-scale density matrix renormalization group calculations, we show that this remarkable quantum phase is the ground state of a reasonable microscopic Hamiltonian-the usual *t*-*J* model with electron kinetic energy *t* and two-spin exchange *J* supplemented with a frustrated electron 'infig-exchange' term, which we here examine extensively on the square lattice two-leg ladder. These findings constitute an explicit theoretical example of a grouine non-fermi-liquid metal existing as the ground state of a realstic model.

Motivation



Chandra Varma, Nature 468, 184-185 (11 November 2010)

- Anisotropic resistivity ρ: effective 2D description
- $\rho \propto T$ in contrast to $\rho \propto T^2$ for Fermi liquid
- violation of Luttingers volume theorem

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 different experiments: different total amount of charge carriers

t-j-K model





$$\begin{split} H &= H_{tJ} + H_{K} \\ H_{tJ} &= -t \sum_{\langle i,j \rangle, s=\uparrow\downarrow} \left(c_{is}^{\dagger} c_{js} + c_{js}^{\dagger} c_{is} \right) + J \sum_{\langle i,j \rangle} \mathbf{S}_{i} \cdot \mathbf{S}_{j} \\ H_{K} &= 2K \sum_{\Box} \left(S_{13}^{\dagger} S_{24} + S_{24}^{\dagger} S_{14} \right) \\ S_{ij}^{\dagger} &= \frac{1}{\sqrt{2}} \left(c_{i\uparrow}^{\dagger} c_{j\downarrow}^{\dagger} - c_{i\downarrow}^{\dagger} c_{j\uparrow}^{\dagger} \right) \end{split}$$

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slave-boson technique for d-wave metal

 electron operator can be written as product of charge carrying slave boson (chargon) and spin-half fermionic spinon

 $c_s(\mathbf{r}) = b(\mathbf{r}) f_s(\mathbf{r})$

- $b(\mathbf{r})$ is given by a d-wave Bose-metal wavefunction
- $f_s(\mathbf{r})$ is given by a Slater determinant
- Use a constraint so the Hilbert space does not change size:

$$b^{\dagger}(\mathbf{r})b(\mathbf{r}) = \sum_{s} f_{s}^{\dagger}(\mathbf{r})f_{s}(\mathbf{r}) = \sum_{s} c_{s}^{\dagger}(\mathbf{r})c_{s}(\mathbf{r}) = n_{e}(\mathbf{r})$$

- This is achieved by strongly coupling b(r) and f_s(r) via an emergent gauge field
- The Bose-metal itself consists of two fermionic slave particles (partons) b(r) = d₁(r)d₂(r) coupled via a gauge field to implement the constraint:

$$d_1^{\dagger}(\mathbf{r})d_1(\mathbf{r}) = d_2^{\dagger}(\mathbf{r})d_2(\mathbf{r}) = b^{\dagger}(\mathbf{r})b(\mathbf{r})$$

Mean-field solution

- ▶ Project 2D system on quasi-1D ladder geometry. In this case a two-leg ladder with up to $L_x = 48$ sites in length and electron density $\rho = 1/3$.
- in mean-field approximation: 5 1D gapless modes $\int_{-\pi}^{d_1} \int_{k_{k_{e_n}}^{0} k_{e_n}^{(0)}} \int_{-\pi}^{d_1} \int_{k_{k_{e_n}}^{0} k_{k_{e_n}}^{(0)}} \int_{-\pi}^{d_2} \int_{k_{k_{e_n}}^{0} k_{e_n}}^{d_2} \int_{-\pi}^{d_1} \int_{k_{k_{e_n}}^{0} k_{e_n}}^{d_2} \int_{-\pi}^{d_2} \int_{k_{k_{e_n}}^{0} k_{e_n}}^{d_2} \int_{-\pi}^{d_2} \int_{k_{k_{e_n}}^{0} k_{e_n}}^{d_2} \int_{-\pi}^{d_2} \int_{k_{k_{e_n}}}^{d_2} \int_{-\pi}^{d_2} \int_{-\pi}^{d$
- Because of the constraints: $k_{Fd1}^{(0)} + k_{Fd1}^{(\pi)} = k_{Fd2} = 2k_{Ff} = 2\pi\rho$

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Gauge theory description + solution using bosonization

Kinetic energy density (linearized) in the parton language:

$$h_{kinetic} = \sum_{k_y=0,\pi} \sum_{P=R/L} Pv_{d1}^{(k_y)} d_{1P}^{(k_y)\dagger} (-i\partial_x) d_{1P}^{(k_y)}$$
$$+ \sum_{P=R/L} Pv_{d2} d_{2P}^{\dagger} (-i\partial_x) d_{2P} + \sum_{s=\uparrow,\downarrow} \sum_{P=R/L} Pv_f f_{sP}^{\dagger} (-i\partial_x) f_{sP}$$

Bosonize the fields:

$$d_{1P}^{(0)} = \eta_{d_1^{(0)}} e^{i\left(\varphi_{d_1^{(0)}} + P\theta_{d_1^{(0)}}\right)}, \dots$$

Bosonize the interaction terms as well

$$\begin{aligned} h_{int,4d_1} &= \omega \left[d_{1R}^{(0)\dagger} d_{1L}^{(0)\dagger} d_{1L}^{(\pi)} d_{1R}^{(\pi)} + H.c. \right] = 2\omega \cos \left[2\sqrt{2}\varphi_{d1-} \right] \\ h_{int,4f} &= -u \left(f_R^{\dagger} \frac{\vec{\sigma}}{2} f_R \right) \cdot \left(f_L^{\dagger} \frac{\vec{\sigma}}{2} f_L \right) \\ &= \frac{u^z}{8\pi^2} \left[(\partial_x \varphi_{f\sigma})^2 - (\partial_x \theta_{f\sigma})^2 \right] + u^{\perp} \cos(2\sqrt{2}\theta_{f\sigma}) \end{aligned}$$

• After bosonization, the constraint is simply: $\theta_{d1}^{(0)} + \theta_{d1}^{(\pi)} = \theta_{d2} = \theta_{f\uparrow} + \theta_{f\downarrow}$

 \blacktriangleright perform an orthonormal transformation on the θ and φ fields:

$$\begin{aligned} \theta_{f\sigma} &= \frac{1}{\sqrt{2}} (\theta_{f\uparrow} - \theta_{f\downarrow}) \\ \theta_{d1-} &= \frac{1}{\sqrt{2}} (\theta_{d1}^{(0)} - \theta_{d1}^{(\pi)}) \\ \theta_{\rho tot} &= \frac{1}{2\sqrt{2}} (\theta_{f\uparrow} + \theta_{f\downarrow} + \theta_{d1}^{(0)} + \theta_{d1}^{(\pi)} + 2\theta_{d2}) \\ \theta_{a} &= \frac{1}{\sqrt{3}} (\theta_{d1}^{(0)} + \theta_{d1}^{(\pi)} - \theta_{d2}) \\ \theta_{A} &= \frac{\sqrt{3}}{2\sqrt{2}} \left(\theta_{f\uparrow} + \theta_{f\downarrow} - \frac{\theta_{d1}^{(0)} + \theta_{d1}^{(\pi)} + 2\theta_{d2}}{3} \right) \end{aligned}$$

 Gauge field fluctuations render the θ_a, θ_A fields massive: only 3 modes remain



$$K_e = \pm \left(k_{Fd1}^{(0,\pi)} - \pi \rho \right)$$

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DMRG phase diagram



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DMRG expectation values





Conclusion

- A two-leg ladder model to describe the strange metal phase is introduced
- It shows strong non-Fermi-liquid behaviour
- The model is to some extend analytically accessible using slave-boson technique and bosonization
- The two-leg ladder d-wave metal is extendable to systems with more legs.
- The d-wave symmetry of its metallic phase suggests that there may be incipient d-wave superconductivity

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