

Direct measurement of the Zak phase in topological Bloch bands

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Geometric phases that characterize the topological properties of Bloch bands play a fundamental role in the band theory of solids. Here we report on the measurement of the geometric phase acquired by cold atoms moving in one-dimensional optical lattices. Using a combination of Bloch oscillations and Ramsey interferometry, we extract the Zak phase—the Berry phase gained during the adiabatic motion of a particle across the Brillouin zone—which can be viewed as an invariant characterizing the topological properties of the band. For a dimerized lattice, which models polyacetylene, we measure a difference of the Zak phase $\delta\varphi_{\text{Zak}} = 0.97(2)\pi$ for the two possible polyacetylene phases with different dimerization. The two dimerized phases therefore belong to different topological classes, such that for a filled band, domain walls have fractional quantum numbers. Our work establishes a new general approach for probing the topological structure of Bloch bands in optical lattices.

Franziska Maier

Dec 17, 2013

Introduction

Topological phenomena:

- Fermion number fractionalization
- Integer Quantum Hall effect
- Protected surface states

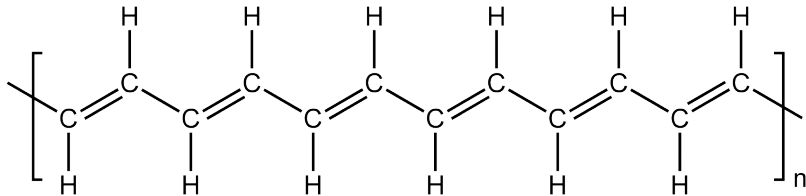
Topological invariants:

- (2D) Chern number – related to Berry's phase
- (1D) e.g. Zak phase to define invariants

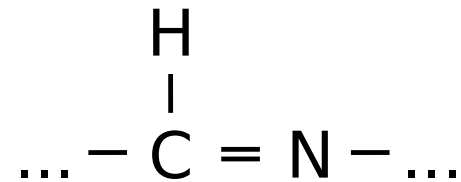
Systems with non-trivial Zak phase:

Polyacetylene (Su-Schrieffer-Heeger model)

Linearly conjugated diatomic polymers



en.wikipedia.org



Idea:

Measure Zak phase using Bloch oscillations and Ramsey interferometry
in 1D optical lattices

Definition Zak phase

$$\varphi_{\text{Zak}} = i \int_{-G/2}^{G/2} \langle u_k | \partial_k | u_k \rangle dk$$

Cell periodic Bloch function:

$$u_k(x) = e^{-ikx} \psi_k(x)$$

Reciprocal lattice vector:

$$G = 2\pi/d$$

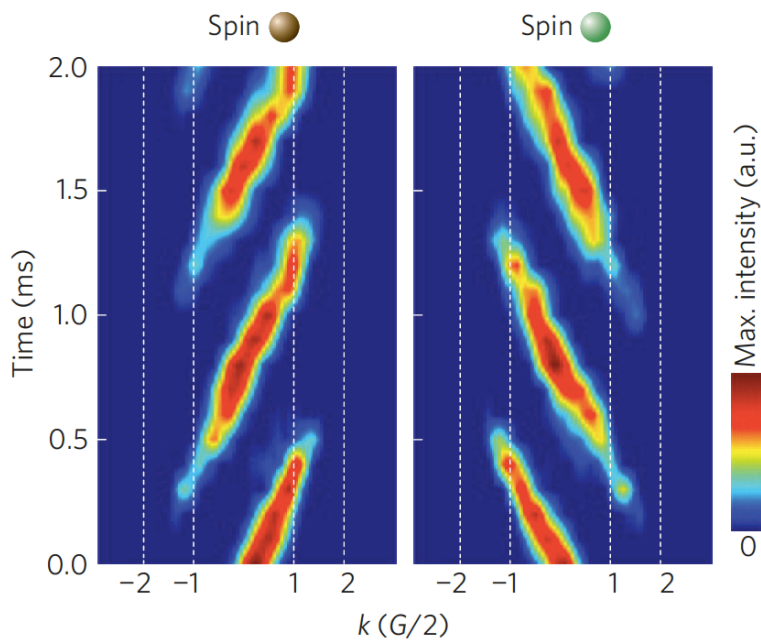
Depends on choice of unit cell, relative phase is well defined



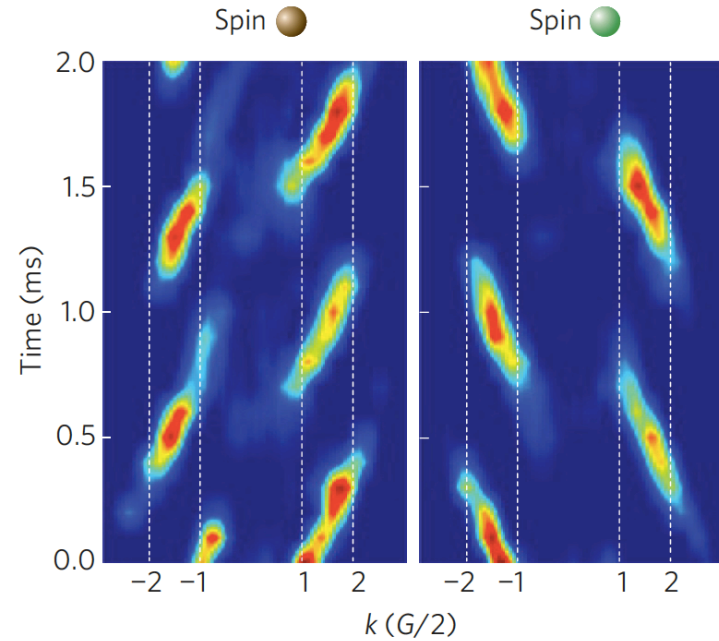
J. Zak, PRL 62, 2747 (1989)

Bloch oscillations - TOF distributions

Move particles adiabatically through Brillouin zone using Bloch oscillations.



Lower band



Upper band

$$\tau_{\text{Bloch osc.}} \sim 850 \mu\text{s}$$

Dimerized optical lattice

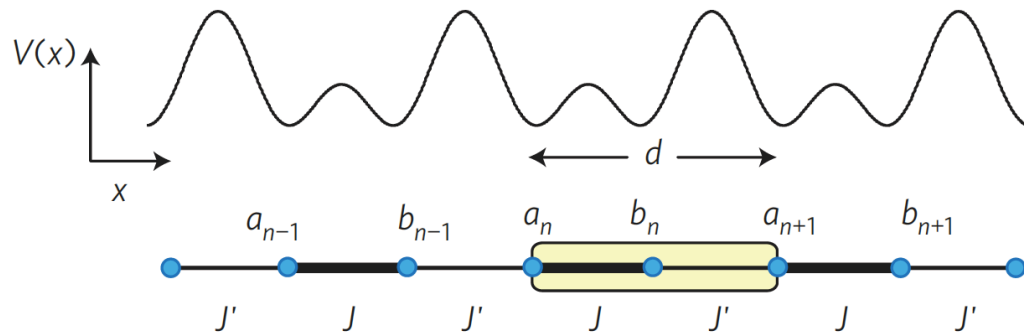
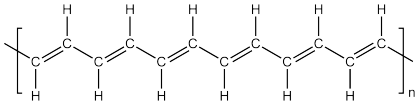
Rice-Mele Hamiltonian

$$\hat{H} = - \sum_n (J \hat{a}_n^\dagger \hat{b}_n + J' \hat{a}_n^\dagger \hat{b}_{n-1} + \text{h.c.}) + \Delta \sum_n (\hat{a}_n^\dagger \hat{a}_n - \hat{b}_n^\dagger \hat{b}_n)$$

PRL 49, 1455 (1982)

$$\Delta = 0$$

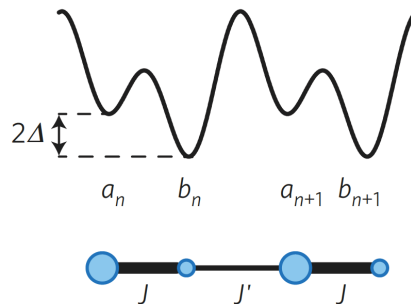
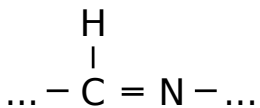
Polyacetylene



$D1, J > J'$
 $D2, J < J'$

$$\Delta \neq 0$$

Linearly conjugated diatomic polymer



Realizing the lattice

Load Bose-Einstein condensate of $\sim 5 \times 10^4$ ^{87}Rb atoms
in 1D optical superlattice defined by

$$V(x) = V_l \sin^2(k_l x + \phi/2) + V_s \sin^2(2k_l x + \pi/2)$$

$$\phi = 0 \rightarrow D1$$

$$\phi = \pi \rightarrow D2$$

$$\phi \neq 0, \pi \rightarrow \text{control } \Delta$$

$$\lambda_s = \lambda_l/2 = 767 \text{ nm}$$

$$k_l = 2\pi/\lambda_l$$

Eigenstates of H

Wannier functions

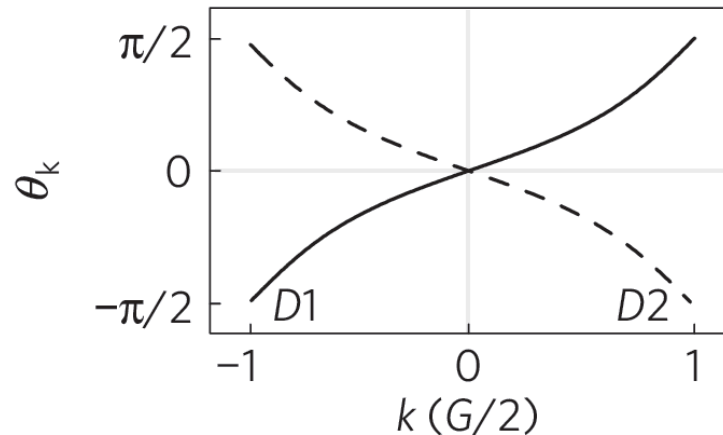
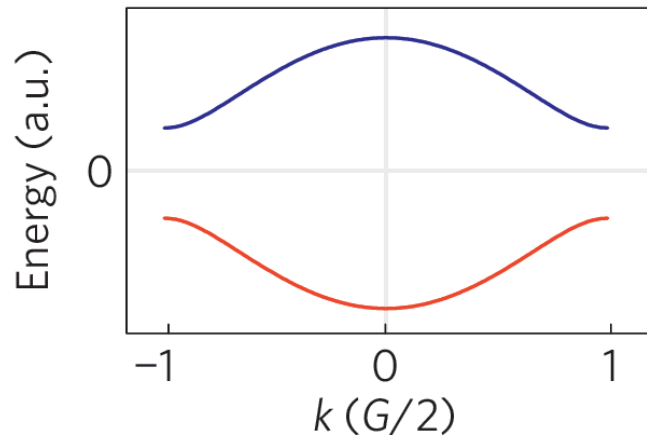
$$\psi_k(x) = \sum_n \alpha_k e^{ikx_n} w_a(x - x_n) + \beta_k e^{ik(x_n + d/2)} w_b(x - x_n - d/2)$$

Pseudospin vektor

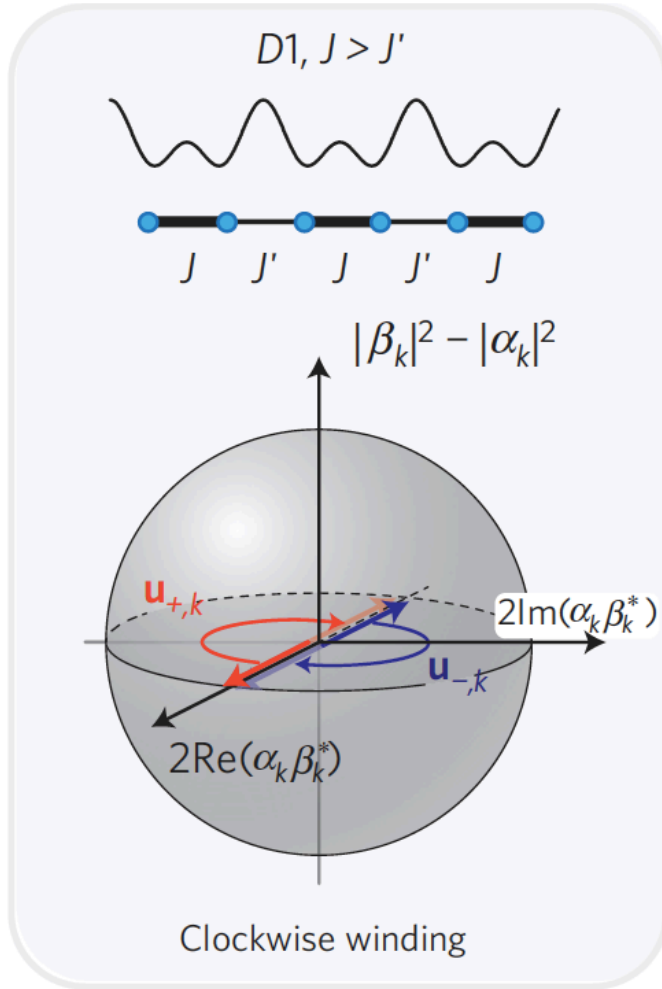
$$\mathbf{u}_k = (\alpha_k, \beta_k)$$

$$\Delta = 0 \quad \mathbf{u}_{\mp, k} = \frac{1}{\sqrt{2}} \begin{pmatrix} \pm 1 \\ e^{-i\theta_k} \end{pmatrix}$$

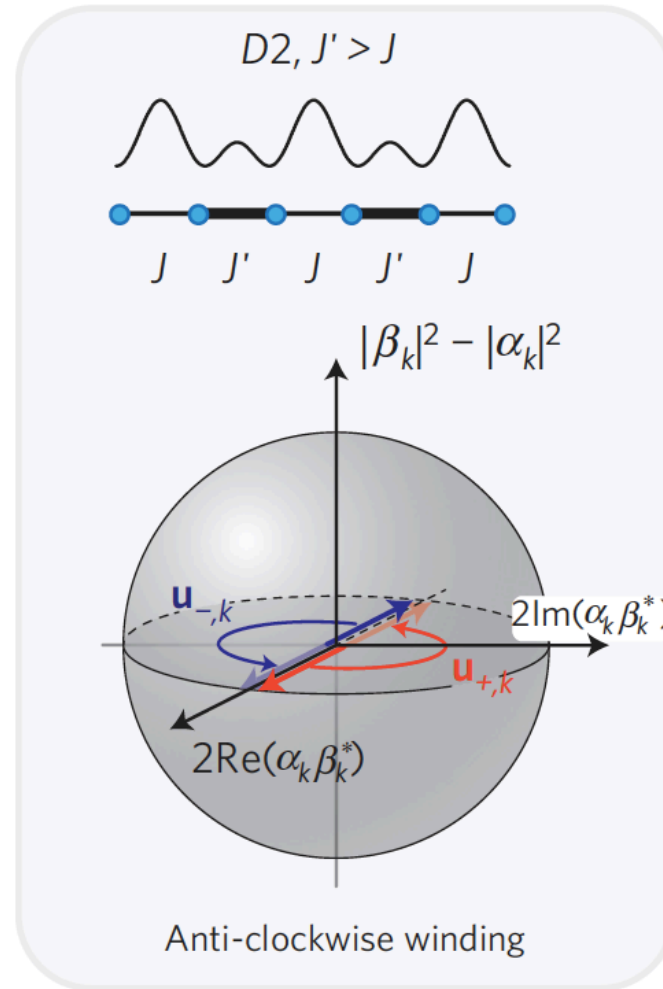
$$J e^{ikd/2} + J' e^{-ikd/2} = |\epsilon_k| e^{i\theta_k}$$



Pseudospin representation $\Delta = 0$



$$\varphi_{\text{Zak}}^{D1} = \pi/2$$



$$\varphi_{\text{Zak}}^{D2} = -\pi/2$$

Phase dependent winding direction of \mathbf{u}

Phase Shift - 3Step Sequence I

Phase due to adiabatic movement in Brillouin zone:

$$\varphi_{\text{tot}} = \varphi_{\text{Zak}} + \varphi_{\text{dyn}} + \varphi_{\text{Zeeman}}$$

3step sequence to isolate $\delta\varphi_{\text{Zak}}$
(one atom)

1) $|\downarrow, k = 0\rangle$

MW pulse $\xrightarrow{\pi/2}$ $1/\sqrt{2}(|\downarrow, k = 0\rangle + |\uparrow, k = 0\rangle)$

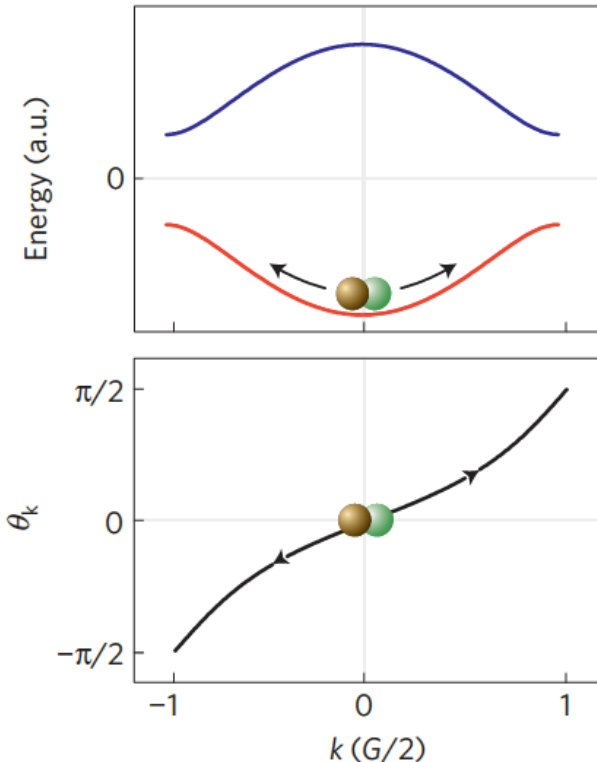
Bloch oscillations due to a **B**-field gradient

$$1/\sqrt{2}(e^{i\delta\varphi} |\downarrow, -k\rangle + |\uparrow, k\rangle)$$

①

Bloch oscillation
 $D1, J > J'$

MW pulse and phase $\left[\begin{array}{c} \pi/2, 0 \end{array} \right] \dots$



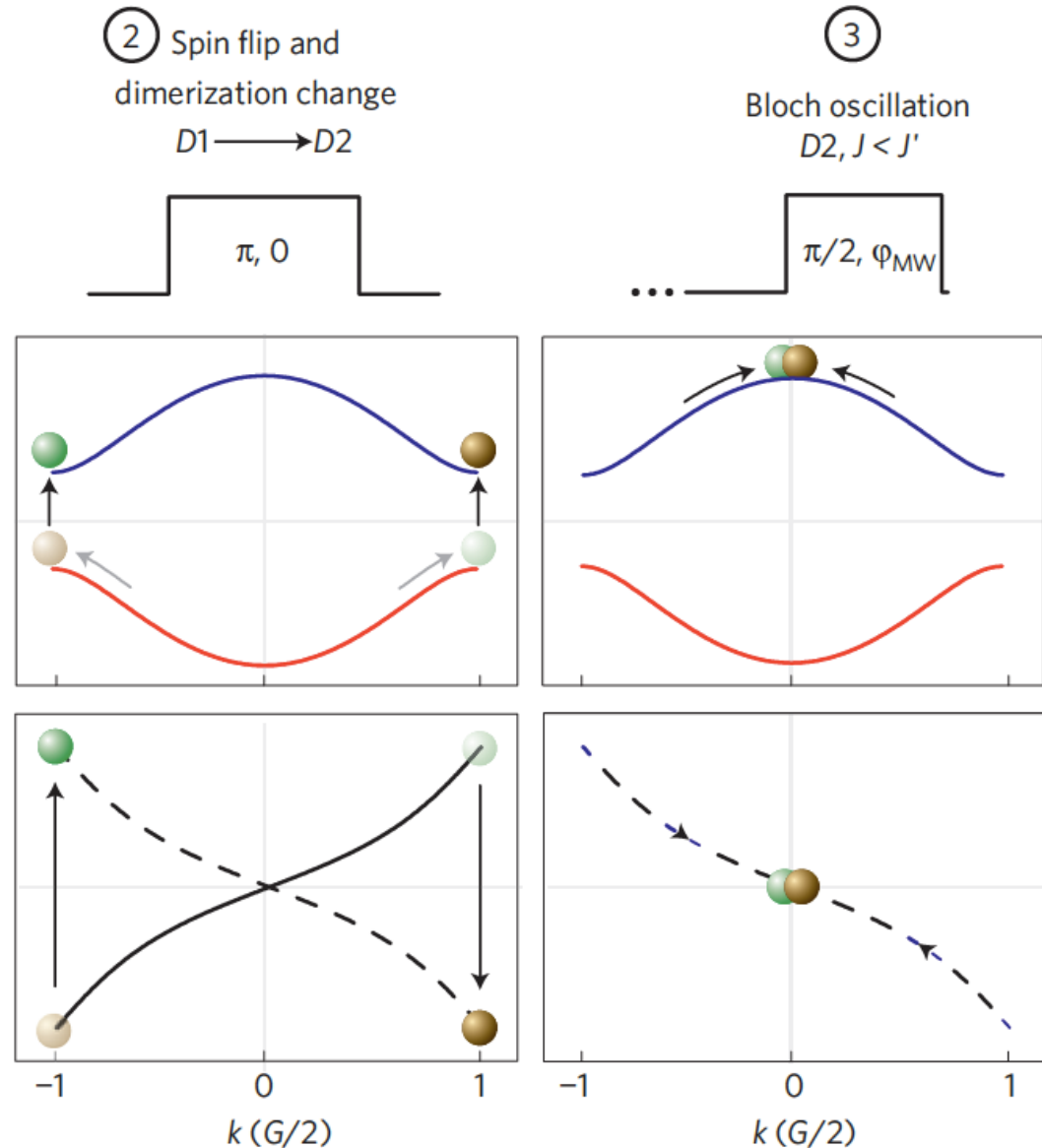
Phase Shift - 3Step Sequence II

2) Eliminate $\delta\varphi_{\text{Zeeman}}$ by a spin echo π pulse and add a **non-adiabatic dimerization swap**
 $D1 \rightarrow D2$

3) Evolutions via Bloch oscillations back to $k = 0$
 Interference of the two spin components with MW $\pi/2$ pulse

TOF measurements with Stern-Gerlach setup separates spin states and reveals

$$\delta\varphi = \varphi_{\text{Zak}}^{D1} - \varphi_{\text{Zak}}^{D2}$$

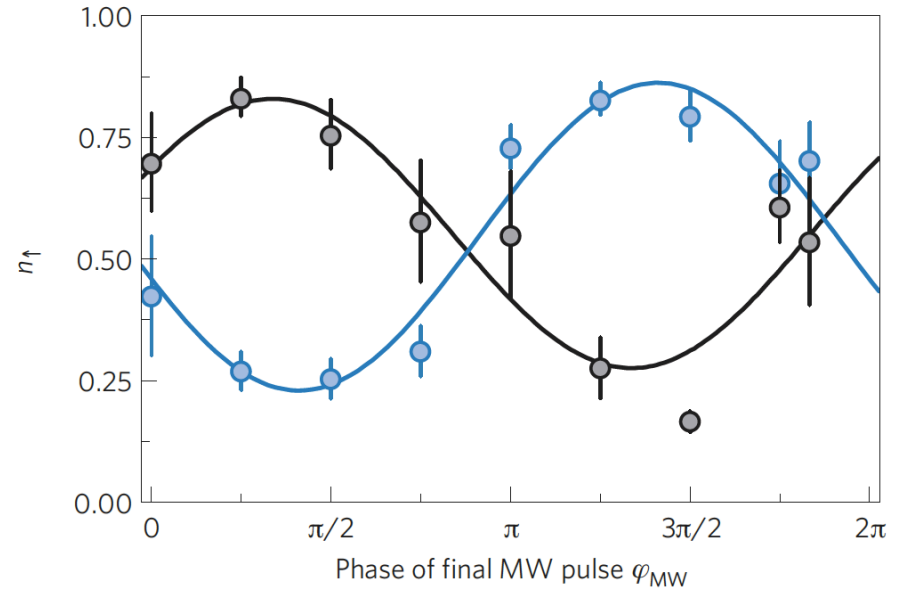


Measured Ramsey Fringes

$$n_{\uparrow} = N_{\uparrow}/N_{\text{total}}$$

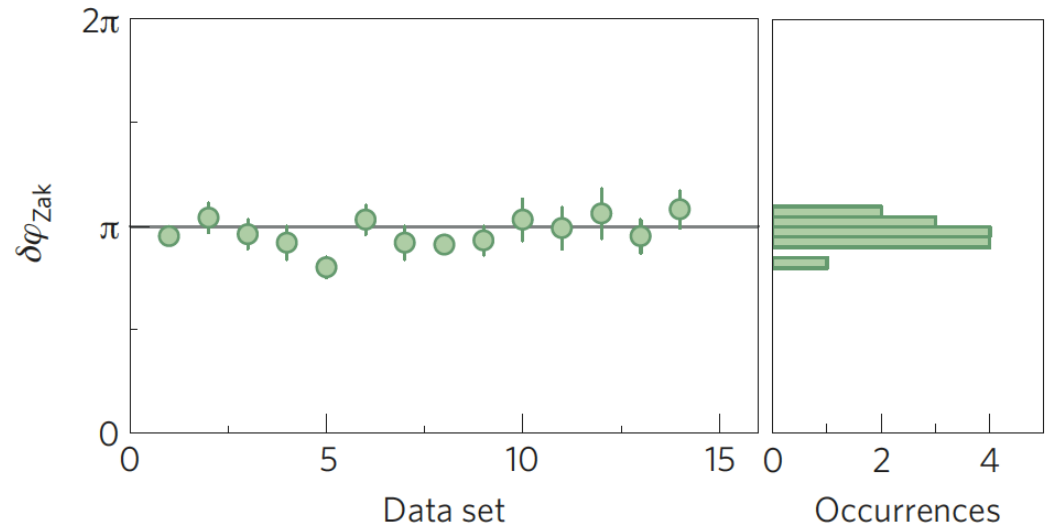
Blue – dimerization swapped

Black – dimerization not swapped

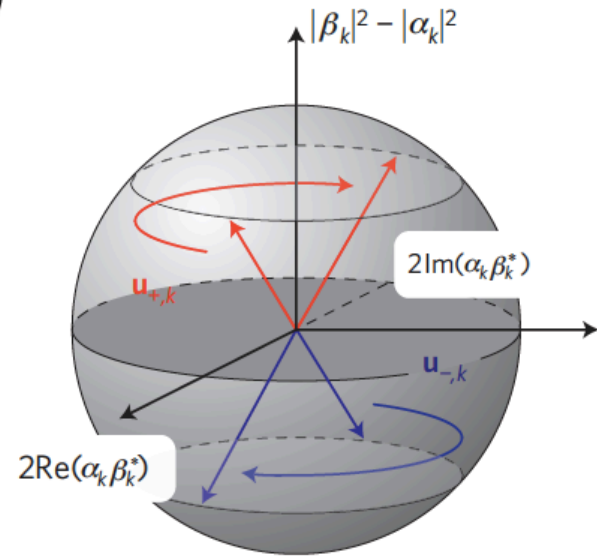
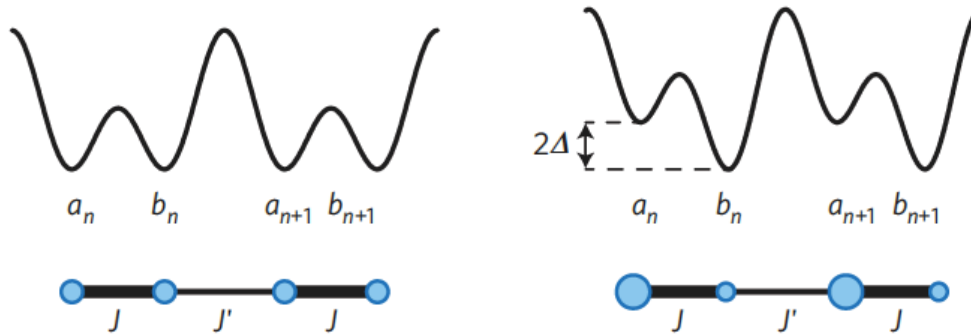


Histogram of
14 measurements

$$\delta\varphi_{\text{Zak}} = 0.97(2)\pi$$



Fractional Zak phase $\Delta \neq 0$

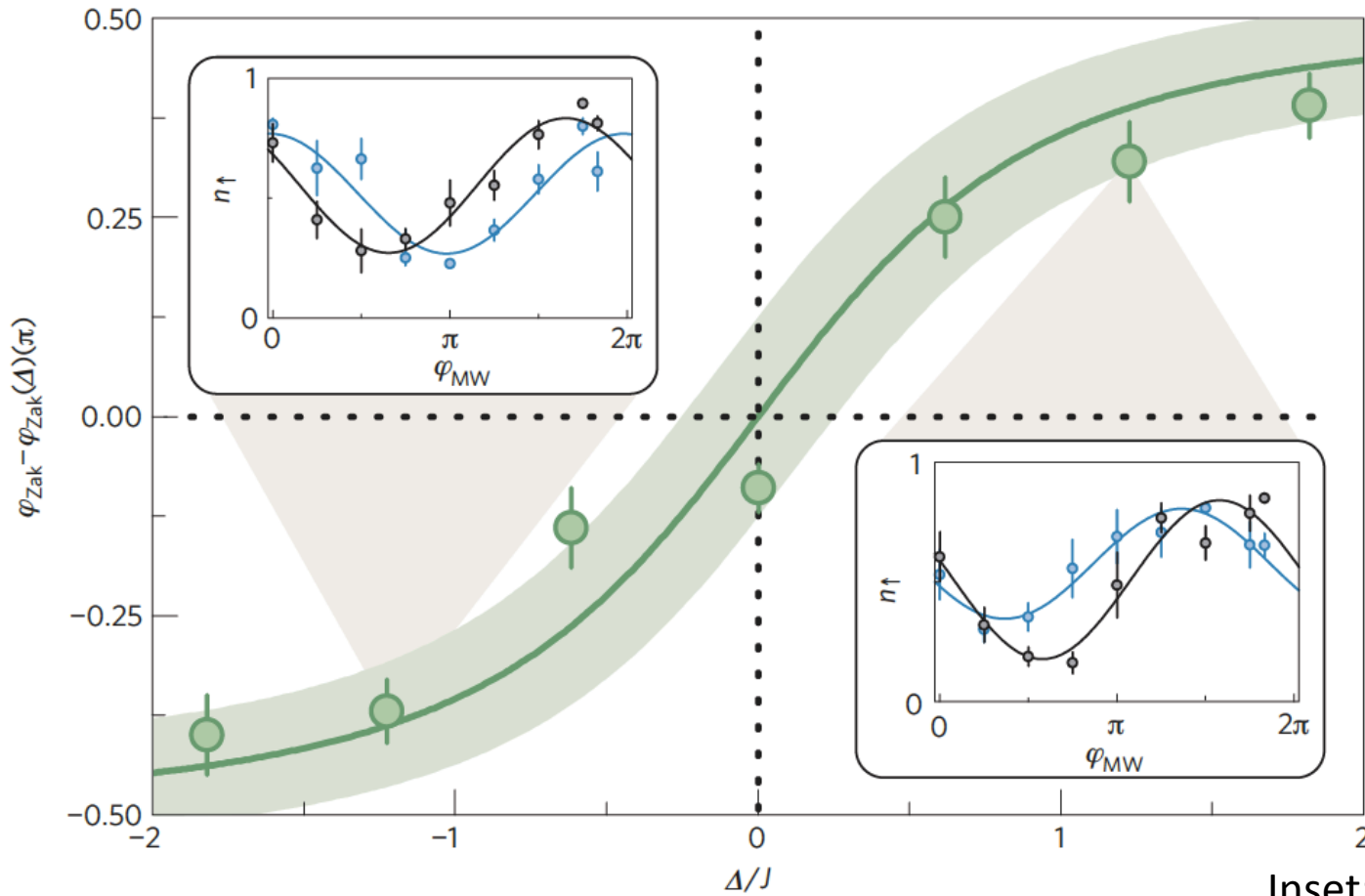


Modified 3step sequence:

$$\Delta = 0 \rightarrow |\Delta| < 2J$$

$$\varphi_{\text{Zak}} = \pi/2 \rightarrow \varphi_{\text{Zak}}(\Delta)$$

Fractional Zak phase



Inset:
Ramsey Fringes
Blue – staggered
Black – not staggered

Conclusions

- Approach
- predict
- Extend
- Next st
- Introdu

