Topologically protected spin and valley currents via mass inversion in Dirac materials

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Journal Club

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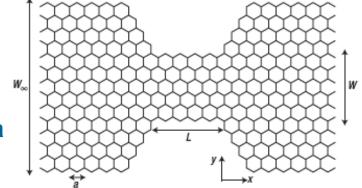
Outline of the talk

- **♦** Introduction
- ◆ General idea: Dirac materials with mass gap
- **♦** Examples: Silicene and MoS2
- Conclusion

Introduction

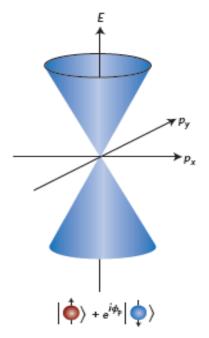
Valleytronics:

A key ingredient for 'valleytronics' would be a controllable way of occupying a single valley in graphene, thereby producing a valley polarization.



Nat. Phys. 3, 172 (2007)

Spintronics:



Topological insulator surface states are described by 2D Dirac equation with strong coupling between electron spin and momentum due to spin-orbit coupling

Nat. Mat. 11, 409 (2012)

General idea

Dirac Hamiltonian with a mass gap

$$H = \hbar v(\hat{k}_x \tau_x + \hat{k}_y \tau_y) + \Delta \tau_z$$

Chern number (integral of the Berry curvature over the Brillouin zone)

$$C(\Delta) = \frac{1}{4\pi} \left(\int_0^{\Lambda} d^2 \vec{k} + \int_{|k| > \Lambda} d^2 \vec{k} \right) \epsilon^{\mu\nu\lambda} \bar{d}_{\mu} \partial_{k_x} \bar{d}_{\nu} \partial_{k_y} \bar{d}_{\lambda}$$
$$= C^{(1)}(\Delta, \Lambda) + C^{(2)}(\Delta, \Lambda) .$$

contributions from wave vectors near to the gapless point





contributions from the rest of the Brillouin zone where we assume there are no further gap closings

Change in Chern number

$$\delta C = C^{(1)}(\Delta) - C^{(1)}(-\Delta)$$

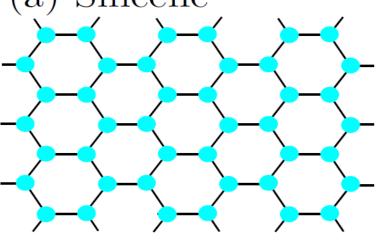
In the limit $\Delta \to 0$ and $\Lambda \gg \Delta/(\hbar v)$

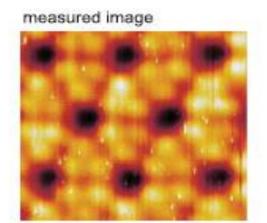
$$\delta C = \frac{1}{4\pi} \int_0^{\Lambda} \frac{2\hbar^2 v^2 \Delta}{(\hbar^2 v^2 |\vec{k}|^2 + \Delta^2)^{3/2}} d^2k = 1$$

Therefore, since there is a change in the Chern number when the sign of Δ is reversed, the boundary between regions of a system with $\Delta > 0$ and $\Delta < 0$ hosts a topologically protected interface state.

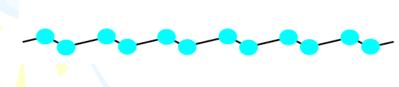
Silicene

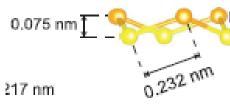
(a) Silicene

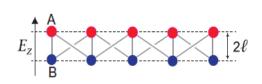




PRL 108, 155501 (2012)







$$H_{\xi s}^{\text{Sil}} = \hbar v (\hat{k}_x \tau_x - \xi \hat{k}_y \tau_y) + \xi s \lambda_{SO} \tau_z + \frac{lE_z}{2} \tau_z$$

Spin
$$s=\pm 1$$
 Valley $\xi=\pm 1$

Low energy Dirac theory

$$\mathcal{E}_{\eta} = \pm \sqrt{\hbar^2 v_{\rm F}^2 k^2 + \left(\ell E_z - s \sqrt{\lambda_{\rm SO}^2 + a^2 \lambda_{\rm R}^2 k^2}\right)^2} \qquad s = \eta s_z$$

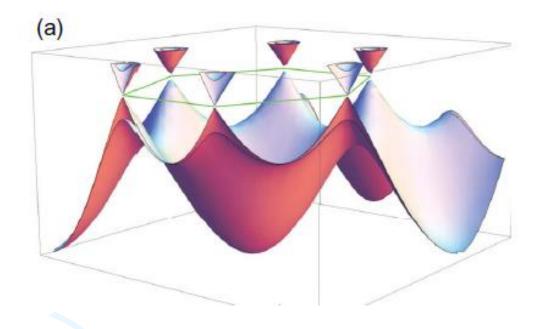


Figure 3. Band structure of silicene at the critical electric field E_c . (a) A bird's-eye view. Dirac cones are found at six corners of the hexagonal Brillouin zone.

For k=0

$$\Delta (E_z) = 2 |\ell E_z - \eta s_z \lambda_{SO}|$$

$$E_{\rm c} = \lambda_{\rm SO}/\ell = 17 \,\mathrm{meV\, \mathring{A}}^{-1}$$
.

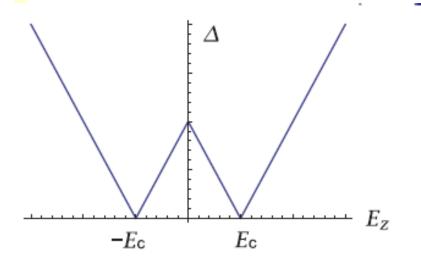


Figure 2. The band gap Δ as a function of the electric field E_z . The gap is open for $E_z \neq \pm E_c$, where silicene is an insulator. It can be shown that it is a topological insulator for $|E_z| < E_c$ and a band insulator for $|E_z| > E_c$.

Inhomogeneous electric field
$$\longrightarrow$$
 $E_z = x\mathcal{E}/R$

$$\Delta < 0$$
 when $lE_z(x) < -\xi s\lambda$, otherwise $\Delta > 0$

For $\xi s = 1$, two interface modes near $x = -\lambda R/(\mathcal{E}l)$

For $\xi s = -1$, two interface modes near $x = \lambda R/(\mathcal{E}l)$

Spectral asymmetry

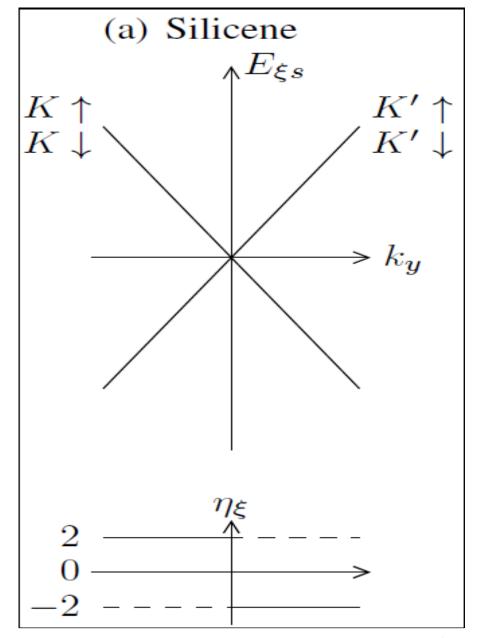
$$\eta_s = \frac{2}{\sqrt{\pi}} \operatorname{Tr} \int_0^\infty \operatorname{He}^{-y^2 H^2} P_s dy ,$$

$$\eta_{\xi} = \frac{2}{\sqrt{\pi}} \operatorname{Tr} \int_0^\infty \operatorname{He}^{-y^2 H^2} P_{\xi} dy ,$$

$$\eta_K = 2\mathrm{sgn}(k_y)$$

$$\eta_{K'} = -2\mathrm{sgn}(k_y)$$

This index indicates that there is a fundamental asymmetry in the valley distribution of the interface modes in silicene.



Dispersion of the interface modes

$$\varepsilon_{\xi s}^{\rm Sil} = -\xi \hbar v k_y$$

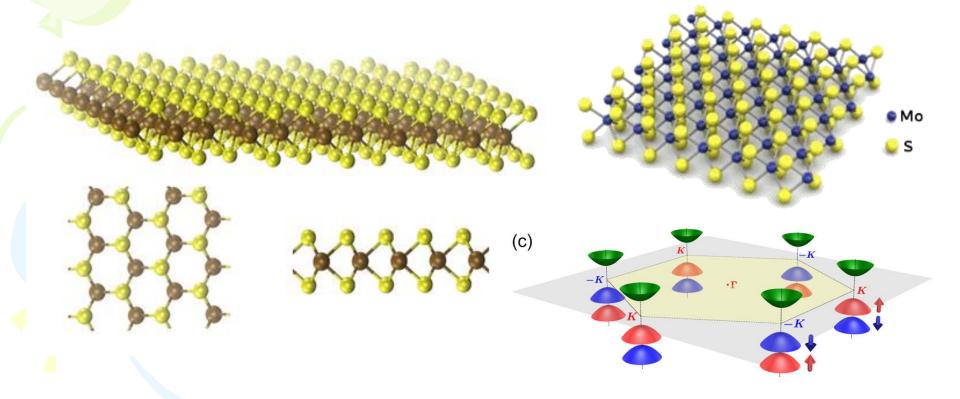
Spin and Valley current

$$v_{K\uparrow}=v_{K\downarrow}=-\hbar v$$
 Left moving $v_{K'\uparrow}=v_{K'\downarrow}=\hbar v$ Right moving

$$j_{\xi s} = \frac{1}{2\hbar k_c} \int_{-k_c}^{k_c} dk_y v_{\xi s} n_{\xi s} \qquad v_{\xi s} = d\varepsilon_{\xi s}^{\text{Sil}} / dk_y$$

$$j_{s} = j_{K\uparrow} + j_{K'\uparrow} - j_{K\downarrow} - j_{K'\downarrow}, \qquad j_{s} = 0$$
$$j_{\xi} = j_{K\uparrow} + j_{K\downarrow} - j_{K'\uparrow} - j_{K'\downarrow}, \qquad j_{\xi} = -2\hbar v$$

MoS_2



$$H_{\xi s}^{\text{TMD}} = \hbar v (\xi k_x \tau_x + k_y \tau_y) + \frac{\Delta}{2} \tau_z - \frac{\xi s \lambda}{2} (\tau_z - \tau_0)$$

Inhomogeneous mass term \longrightarrow $\Delta(x) = \Delta_0 x/R$



Dispersion of the interface modes

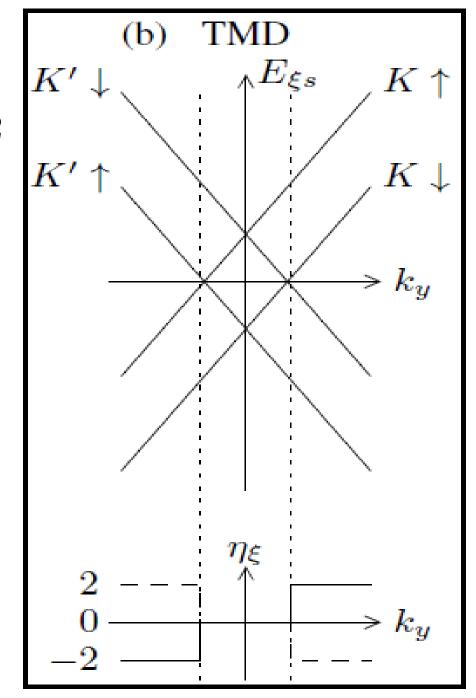
$$\varepsilon_{\xi s}^{\text{MoS2}} = \xi \hbar v k_y + \xi s \lambda / 2$$

Valley current

$$j_{\xi} \approx 2v$$

Spin current

$$j_s \approx -\lambda$$



Conclusions



- Pseudo-spin polarized currents by topologically protected modes created by mass inversion
- Silicene: interface modes carry valley current
- → MoS2: exhibit both spin and valley currents at interfaces
- Short range scatterers can introduce inter valley scattering which can destroy such interface modes

